

March 23, 2015
 * DE & MO & clve
 Friday
 * Quiz #7 - Friday

Mar 23-10:53 AM

Rational Exponents
 Let $(x)^4 = (3^{\frac{1}{4}})^4$
 $x^4 = 3^{\frac{4}{4}} = 3^1 = 3$
 $x^4 = 3$
 This means that some number "x" raised to the fourth power is 3.
 $\sqrt[4]{x^4} = \sqrt[4]{3}$
 $x = \sqrt[4]{3}$
 So:
 ① $x = 3^{-1/4}$
 ② $x = \sqrt[4]{3}$
 then $3^{\frac{1}{4}} = \sqrt[4]{3}$
 (Note: "pull" and "check" annotations in the original image)

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rules
 ① $a^{-\frac{m}{n}} = \sqrt[n]{a^m}$
 ② $a^{-\frac{m}{n}} = \frac{1}{a^{\frac{m}{n}}} = \frac{1}{\sqrt[n]{a^m}}$
 ③ $\frac{1}{a^{-\frac{m}{n}}} = a^{\frac{m}{n}} = \sqrt[n]{a^m}$

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$\sqrt[2]{4^1} = 4^{1/2} = 2$
 because $2^2 = 4$
 $64^{2/3} = \sqrt[3]{64^2} = \sqrt[3]{64}$
 $= \sqrt[3]{(4)^3}$
 $= 4$

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long way $8^{2/3} = \sqrt[3]{8^2} = \sqrt[3]{64} = 4$
 alternate way $8^{2/3} = \sqrt[3]{8^2} = (\sqrt[3]{8})^2$
 $= (\sqrt[3]{(2)^3})^2$
 $= 2^2$
 $= 4$

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$64^{2/3} = \sqrt[3]{64^2} = \sqrt[3]{4096} = 16$
 $= (\sqrt[3]{64})^2$
 $= (4)^2$
 $= 16$

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$$\begin{aligned}
 (-27)^{-2/3} &= \frac{1}{(-27)^{2/3}} \\
 &= \frac{1}{\sqrt[3]{(-27)^2}} \\
 &= \frac{1}{\sqrt[3]{(-27)^2}} \quad \text{all way} \\
 &= \frac{1}{(-3)^2} = \boxed{\frac{1}{9}}
 \end{aligned}$$

$(-3)^3 = -27$
 $(-3) \cdot (-3) \cdot (-3)$
 $9 \cdot (-3) = -27$

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$$\begin{aligned}
 7^{1/3} &= 7^{1/3} \\
 7^{3/4} &= 7^{3/4} \\
 7^{1/3} - 7^{3/4} &= 7^{1/3} - 7^{3/4} = \frac{4-9}{12} = -\frac{5}{12} \\
 &= 7^{-5/12} = \boxed{\frac{1}{7^{5/12}}}
 \end{aligned}$$

same base

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$$\begin{aligned}
 x^{2/3} \cdot x^{7/3} &= x^{2/3 + 7/3} = x^{9/3} = x^3 \\
 &= \boxed{x^3} \quad \text{same base} \\
 &\propto \sqrt[15]{x^{18}} \\
 \sqrt{x^2} \cdot \sqrt[3]{x^2} &= x^{1/2} \cdot x^{2/3} = x^{3/6 + 4/6} = x^{7/6} = \sqrt[6]{x^7}
 \end{aligned}$$

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$$\begin{aligned}
 x^{3/6} (x^{1/3} \cdot x^{1/6}) &= x^{3/6 + 1/3 + 1/6} = x^{3/6 + 2/6 + 1/6} = x^{6/6} = x \\
 x^{5/6} (x^{2/3}) &= x^{5/6 + 4/6} = x^{9/6} = x^{3/2} = \sqrt{x^3} \\
 &= x^{20/24 + 29/24} = x^{49/24} = \boxed{x^{49/24}}
 \end{aligned}$$

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Different Analysis!

$$\begin{aligned}
 \frac{\sqrt{x}}{\sqrt[3]{x}} &= \frac{x^{1/2}}{x^{1/3}} \\
 &= x^{1/2 - 1/3} = x^{3/6 - 2/6} = x^{1/6} \\
 &= x^{1/6} = \boxed{\sqrt[6]{x}}
 \end{aligned}$$

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$$\begin{aligned}
 \left(\frac{25}{36}\right)^{3/2} &= \frac{(25)^{3/2}}{(36)^{3/2}} = \frac{\sqrt{25^3}}{\sqrt{36^3}} \\
 &= \frac{(\sqrt{25})^3}{(\sqrt{36})^3} \\
 &= \frac{5^3}{6^3} = \boxed{\frac{125}{216}}
 \end{aligned}$$

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